

Directional oxygen diffusion in $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ crystals for long reversible thermochemistry

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ABSTRACT

Redox activity of metal oxides are the key to the development of high-temperature thermochemical energy storage. However, few studies have reported that the reactivity of metal oxides as thermochemical energy storage is significantly affected by the changes of crystal structure and morphology during redox, caused by ion diffusion and vacancy formation and migration. In this study, we find a previously unreported high-performance thermochemical energy storage material $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ with special structure. $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ shows high energy densities during reduction and oxidation (-219.852 and 207.618 kJ/kg), and keeps 97.06% and 92.98% reactivity after 600 cycles. Voids on specific surfaces are observed after cycling, but not in the fresh sample. We find the voids provide abundant Cu^{2+} , Mn^{4+} species and lattice oxygen to promote its reaction performance. Cu ions migrate obviously after oxidation and molecular dynamics simulations reveal that D_{Cu} (7.4×10^{-14} $\text{cm}^2 \text{s}^{-1}$) is higher than D_{Mn} (5.1×10^{-14} $\text{cm}^2 \text{s}^{-1}$) and D_{O} (1.7×10^{-14} $\text{cm}^2 \text{s}^{-1}$). $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ exhibits voids during oxidation due to ion transport described by the Kirkendall effect. In addition, DFT calculations verify that O^{2-} is more easily to adsorb and diffuse on (111) surface, revealing the optimal transport path and directional diffusion mechanism of O^{2-} . These mechanisms can provide ideas for the reasonable design of materials to improve thermochemical reaction performance.

1. Introduction

As one of the most promising clean technologies in the renewable energy system, the Concentrating Solar Power (CSP) plays an increasingly important role [1,2]. CSP technology equipped with thermal energy storage (TES) can effectively solve the challenge of solar intermittency, shifting electricity production to the most valuable period to provide cost-effective and dispatchable renewable power [3,4]. Among them, thermochemical energy storage (TCES) is considered to be a better fit for the next generation CSP plants due to its advantages of operating at higher temperatures, higher energy density, unlimited transportation distance, and lower heat loss [4,5]. The metal oxide is the most potential candidate for TCES because of its better compatibility with CSP [6]. The metal oxide system based on solid-gas reversible reaction [7] completes the endothermic/exothermic reaction through the desorption/adsorption of oxygen on the material surface and the diffusion in the bulk. However, morphology greatly affects ionic diffusion, it is thus important to understand the morphological evolution of metal

oxides during the redox for the design and development of materials with high performance [8].

Potential representatives of metal oxide systems for high-temperature thermochemical energy storage are $\text{Co}_3\text{O}_4/\text{CoO}$, $\text{Mn}_2\text{O}_3/\text{Mn}_3\text{O}_4$, $\text{CuO}/\text{Cu}_2\text{O}$, and their composites [9,10]. Pure metal oxides have been extensively studied their redox properties and enthalpy of reaction. It was found that $\text{Co}_3\text{O}_4/\text{CoO}$ has good reactivity, but its toxicity and high cost limit the application [7,10–12]. $\text{Mn}_2\text{O}_3/\text{Mn}_3\text{O}_4$ re-oxidation kinetics is slow [10,13,14] and $\text{CuO}/\text{Cu}_2\text{O}$ has serious sintering problems [10,15,16], resulting in poor reaction performance. But they are relatively cheap and have a wide range of resources. And their reaction performance can be improved by adjusting the reaction atmosphere or doping elements [17–23]. Researchers currently focus on the effect of doping modification on material properties and grain growth changes during cycles [18–25]. Liu et al. synthesized Co_3O_4 with different micro-nanostructured morphologies to evaluate their thermochemical energy storage performance [26]. However, the relationship between morphology evolution and ion diffusion during redox, the optimal

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transport path of oxygen ions and their related effect on the chemical properties and performances of materials have not been reported. It is worth noting that ion diffusion in metal oxides plays an important role during redox, accompanied by changes in morphology and structure [8]. Therefore, it is urgent to carry out research and in-depth understanding of these contents to clarify the nature of changes during the redox of metal oxides, thereby broadening the way of performance improvement. In addition, two researchers explored Cu–Mn mixed system for thermochemical energy storage, but both focused on the reactivity of CuMn_2O_4 spinel [27,28]. At present, the use of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ as a thermochemical energy storage material and the study of its reaction performance and evolution mechanism during redox have not been reported.

In this paper, we first discovered the thermochemical energy storage material $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ with special structure and excellent performance. The changes of structure, morphology and surface chemical properties caused by the redox and their effects on the reactivity improvement were analyzed by experimental characterization. The nanostructure formation mechanism and directional oxygen diffusion mechanism in $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ were further discussed by MD simulation and DFT calculation. This study can provide new insights for researchers in related fields to understand the ion and defect diffusion and morphological changes of metal oxides during redox, and guide the preparation and optimal design of thermochemical energy storage materials.

2. Experimental section

2.1. Material preparation

$\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ was synthesized by a simple sol-gel method. $\text{Cu}(\text{NO}_3)_2 \cdot 3\text{H}_2\text{O}$, $\text{Mn}(\text{NO}_3)_2$ with molar ratio of 1:1 were dissolved in appropriate amount of deionized water, and citric acid (metal ions:citric acid = 1:5) was added. The mixture was stirred at 70 °C for 3 h, and then ethylene glycol (citric acid: ethylene glycol = 3: 2) was added and stirred at 90 °C for 2 h. The gel was dried at 200 °C for 3 h and calcined at 450 °C and 900 °C for 4 h, respectively.

2.2. Material characterizations

The phase composition and crystal structures of the various samples at different stages were analyzed by powder X-ray diffraction (XRD). It was performed on an X'Pert Powder diffractometer equipped with $\text{Cu K}\alpha$ radiation source ($\lambda = 1.5406 \text{ \AA}$) operating at 40 kV and 40 mA. The scanning rate was 0.02°, and the range of 2θ was 10–80°. The structural properties of the fresh sample was further identified by Fourier transform infrared (FTIR) spectra on a Thermo Scientific Nicolet iS20 spectrometer using KBr pellets in the range of 4000–400 cm^{-1} with a resolution of 4 cm^{-1} . The X-ray photoelectron spectroscopy (XPS) was used to obtain the information of surface chemistry of products. It was performed on a Thermo Scientific K-Alpha electron energy analyzer with monochromatic $\text{Al K}\alpha$ (1486.6 eV) radiation, which was operated at 15 kV. The peak position of the element was calibrated using the binding energy (BE) of C1s at 284.8 eV. The simultaneous thermal analysis (TGA/DSC3+) was used for measuring the redox performance and energy storage/release density. The test conditions were air atmosphere with a flow rate of 50 mL/min, heating from 50 °C to 1100 °C for reduction and then cooling from 1100 °C–700 °C for oxidation at a heating/cooling rate of 20 °C/min. The micro-morphology, structure and element distribution of the samples were investigated by field emission scanning electron microscopy-energy-dispersive spectroscopy (FESEM-EDS) on a SU-8010 microscope equipped with an Oxford X-max80 spectrometer.

2.3. MD simulations

The molecular dynamics (MD) simulations were performed using a

Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS) [29]. To better describe the inter-atomic interaction of metal oxides, the Matsui-Akaogi (MA) potential was chosen [30]. The system was carried out in the canonical (NVT) ensemble. The simulation temperature and time step were set to 850 °C and 10 ps, respectively. To generate the O concentration gradient, we removed O atoms from the outermost layer.

2.4. DFT calculations

All spin-polarized density functional theory (DFT) calculations were carried out using the Vienna ab initio simulation program (VASP) [31]. The ionic cores were represented by using the projector augmented-wave (PAW) method potentials [32] with the following valence states: 3d10 and 4s1 for Cu, and 3d5 and 4s2 for Mn. Exchange and correlation functions are performed by generalized gradient approximation (GGA) based on functional Perdew-Burke-Ernzerhoff (PBE) approximation [33]. A Hubbard-like model of the GGA + U method [34] was applied to address the strong 3d electron correlations effect of Cu and Mn atoms. For the valence spectra of Mn 3d and Cu 3d levels, the $U = 2.5 \text{ eV}$ was selected accurately to describe the appropriate electronic structure and reaction energetics [35]. The plane wave cut-off energy was set to 450 eV. Spin polarized was used in all calculations. The $(6 \times 6 \times 6)$ Monkhorst-Pack k-point grid was applied for the bulk calculations, while it was set at $4 \times 4 \times 1$ for the surface calculations. For energy calculations, the electronic energy was converged to $1.0 \times 10^{-5} \text{ eV}$, and convergence criterion for internal atomic coordinates until all forces were smaller than 0.025 eV/Å. The lattice constant of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ calculated by DFT was $a = b = c = 8.363 \text{ \AA}$, which was in good agreement with the experimental data ($a = b = c = 8.303 \text{ \AA}$) with small deviations (0.7%). The constructed surface slab model was further expanded into a $p(2 \times 2)$ unit cell, where the vacuum layer was set to 20 Å. The surface slab model consisted of 12 layers of atoms, with six fixed at the bottom and six relaxed at the top. For the energy barrier calculation of ion diffusion, the transition state was optimized by relaxing the force below 0.02 eV/Å using the climbing image nudged elastic band (CI-NEB) method [36].

3. Results and discussion

3.1. Structure characterization of prepared sample

The XRD analysis is performed to determine the crystal structure and phase composition of the prepared sample, and the results are shown in Fig. 1a. All intense diffraction peaks of the sample could be indexed as $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ (ICDD-PDF No. 70–0260), which gave the 2θ values of 18.44°, 30.36°, 35.78°, 37.42°, 43.48°, 48.74°, 54.10°, 57.52°, 63.18° and 75.96°. They corresponded to the (111), (220), (311), (222), (400), (311), (422), (511), (440) and (533) crystal planes of the cubic spinel $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$. Furthermore, the diffraction peaks of the composite were intense, implying good crystallinity. As shown in Fig. 1e, Cu^+ occupies the A site (tetrahedron), while Cu^{2+} and Mn^{4+} occupy the B site (octahedron) in $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ spinel crystal [37]. The Local enlargement FTIR spectra at the range of 1000–400 cm^{-1} have been presented in Fig. 1b. Characteristic bands of around 600 cm^{-1} and 500 cm^{-1} could be attributed to the lattice vibrations of Cu–O in tetrahedral sites (ν_A) and Mn–O in octahedral sites (ν_B) of spinel structure [38], respectively. The cation valence of the sample was identified by XPS. The Cu2p 3/2 spectra is shown in Fig. 1c, where 940–945 eV belongs to vibration satellite peaks [39]. The peak with binding energy at 930.7 eV corresponded to Cu^+ , while the peak at 933.6 eV and satellite peaks belonged to Cu^{2+} [40]. Cu^+ species exists stably because of the interaction between Cu and Mn [41]. Fig. 1d presents the Mn 2p spectra, which there are two main peaks of Mn2p 1/2 and Mn2p 3/2, respectively. The binding energy of Mn 2p3/2 at 640.9 eV and Mn 2p1/2 at 652.6 eV were associated with Mn^{3+} , while the binding energy of Mn 2p3/2 at 642.5 eV and Mn 2p1/2 at 654.2 eV revealed the existence of Mn^{4+} cations [42,

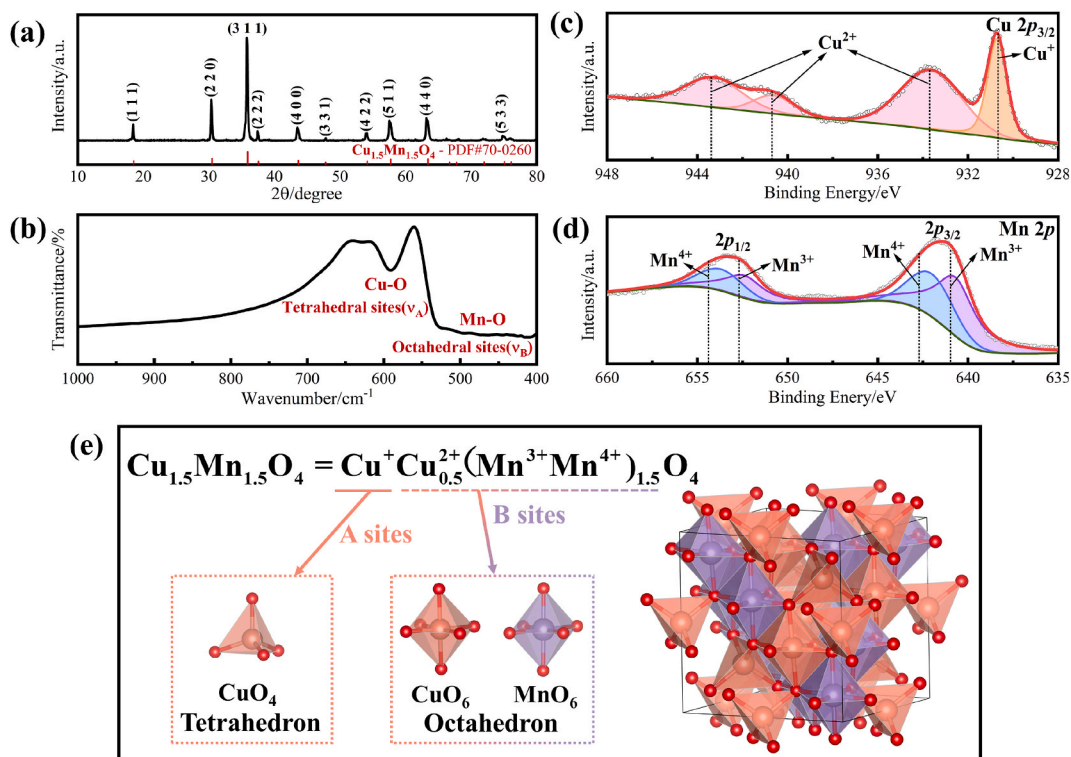


Fig. 1. Characterization of the crystal phase and chemical composition of the fresh sample. (a) XRD pattern. (b) Local enlargement FTIR spectra at the range of 1000–400 cm^{-1} . XPS spectra of (c) Cu 2p_{3/2} and (d) Mn 2p. (e) Schematic of the crystal structure.

43]. Accompanied by the loss of oxygen, part of Mn^{4+} ions are reduced to Mn^{3+} due to the charge neutrality [44]. Obviously, mixed $\text{Cu}^+/\text{Cu}^{2+}$ and $\text{Mn}^{3+}/\text{Mn}^{4+}$ were simultaneously presented in $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ [45]. These results proved that the spinel $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ had been successfully synthesized.

3.2. Reaction performance and cycle stability testing

The redox reactivity and cycle stability of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ is tested by TG/DSC, and the results are presented in Fig. 2. The results of the first cycle are shown in Fig. 2a, the reduction begin at 950 °C, and the peak

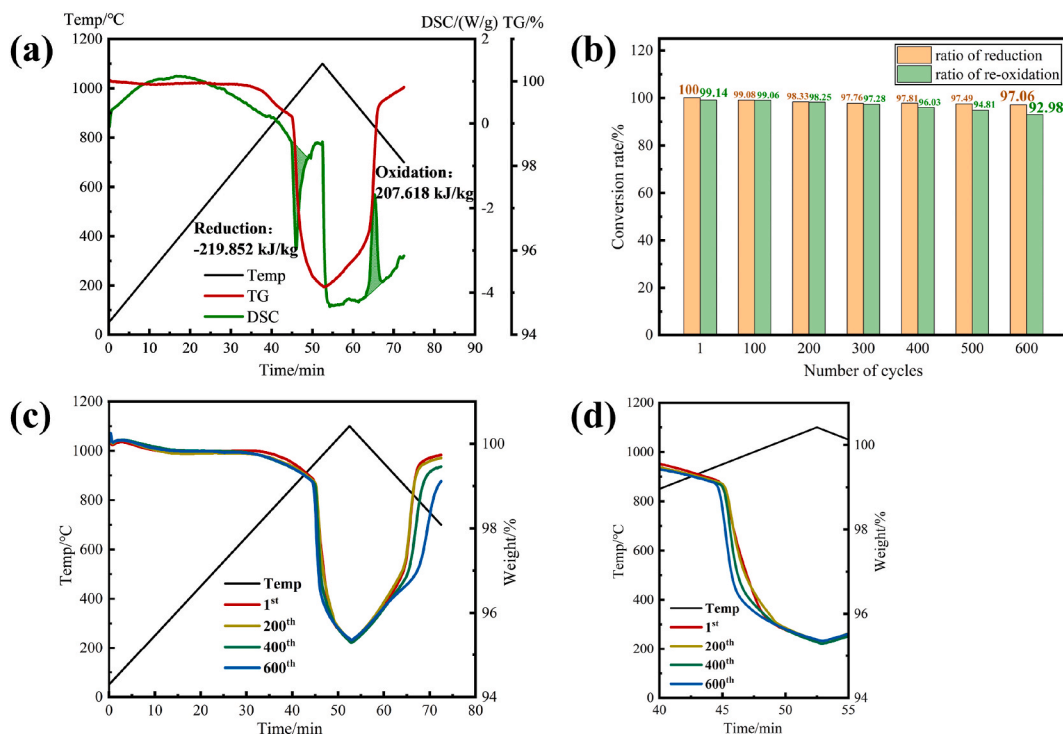


Fig. 2. The excellent performance of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$. (a) First energy storage-release reactivity. (b) Reaction conversion rate during cycle. (c) TG curves at different cycles. (d) Partial TG curves of the reduction in different cycles.

temperature is 970 °C. The weight loss ratio during the reduction was 3.844%, and the thermochemical energy storage density reached -219.852 kJ/kg. The peak temperature during the oxidation was about 850 °C, and the weight gain ratio was 3.811%. The degree of re-oxidation achieved 99%. The energy release density was 207.618 kJ/kg, showing excellent chemical reversibility. Fig. 2b and c demonstrate that the reduction and oxidation conversion rates of Cu_{1.5}Mn_{1.5}O₄ keep 97.06% and 92.98% after 600 cycles, maintaining high reactivity. Based on the same application range, the results of comparing the reaction performance of Mn-based metal oxides are listed in Table 1. The above results showed that Cu_{1.5}Mn_{1.5}O₄ had high energy density and excellent cycle stability. It is worth noting that the slope of TG curve increases with the increase of the number of cycles during the reduction of Cu_{1.5}Mn_{1.5}O₄, indicating that the reduction rate is accelerating (Fig. 2d).

3.3. Evolution of structure and micromorphology during redox

The crystal structure transition process of Cu_{1.5}Mn_{1.5}O₄ during the redox was characterized by XRD. It is worth mentioning that after Cu_{1.5}Mn_{1.5}O₄ was reduced, we used nitrogen atmosphere to prevent it from being oxidized. As shown in Fig. 3a and b, the whole process is mainly composed of spinel Cu_{1.5}Mn_{1.5}O₄ (PDF#70-0262) and layered CuMnO₂ (PDF#50-0860). Cu_{1.5}Mn_{1.5}O₄ released oxygen and stored energy during the reduction, thus transforming into CuMnO₂. The oxidation process occurred reversible reaction, that is, CuMnO₂ completely transformed to Cu_{1.5}Mn_{1.5}O₄, which was consistent with the fresh sample. Therefore, the redox could be described by the following equation.

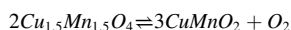


Fig. 3c shows the morphology evolution of Cu_{1.5}Mn_{1.5}O₄ at different stages during redox. The prepared fresh sample presented regular polyhedral shape. However, the reduced CuMnO₂ particles had flake-like morphology of typical delafossite structural materials. Surprisingly, it could be clearly observed that Cu_{1.5}Mn_{1.5}O₄ had special void structure on some surfaces after a complete redox process. The structure was not observed in the fresh sample. It is speculated that the change may be due to the redox of the material, which is related to ions diffusion. In addition, the void structure formation increase the porosity of the material. The effective collision between reacting molecules in unit volume is increased, which is beneficial to promote the chemical reaction. Therefore, the Cu_{1.5}Mn_{1.5}O₄ with void structure exhibits a faster reduction rate in subsequent reduction cycles than the fresh samples, which explains the test results in Fig. 2d.

XPS was used to analyze the surface chemical properties of the materials after morphologic changes. The spectra of Cu 2p_{3/2} and Mn 2p are shown in Fig. 3d and e, respectively. After oxidation, the Cu²⁺ content of Cu_{1.5}Mn_{1.5}O₄ slightly increased from 73.63% to 80.83%,

Table 1

Reduction and oxidation onset temperatures, energy density and cycle performance of Mn-based metal oxides in air.

Metal oxides	T _{red} (°C)	T _{ox} (°C)	Energy density (kJ/kg)	Cycle number
Mn ₂ O ₃ [20]	940	~	-202 and ~	-
94% Mn ₃ O ₄ , 6% SiO ₂ [18]	985	780	-180 and 117	9
95% Mn ₂ O ₃ +5% Cr [19]	972	785	-159.7 and ~	30
(Mn _{0.8} Fe _{0.2}) ₂ O ₃ [20]	978	878	-171.95 and 201.56	100
CuMn ₂ O ₄ +Mn ₃ O ₄ [27]	968	915	~ and 14	5
CuMn ₂ O ₄ +CuO [28]	980	900	~ and 258.32 ± 15.31	20
Cu _{1.5} Mn _{1.5} O ₄	950	890	-219.852 and 207.618	600

~ indicates that this parameter is not given in the reference.

while the Mn⁴⁺ increased from 37.45% to 60.62%, indicating that the void structure formation promoted the oxidation of Cu⁺/Cu²⁺ and Mn³⁺/Mn⁴⁺. Moreover, it is worth noting that it greatly increased the content of Mn⁴⁺, resulting in more exposure of Mn⁴⁺ in the spinel octahedral position to the surface, and significantly, Mn⁴⁺ determined the reactivity [46]. Two typical peaks at 529.6 eV and 530.8 eV in Fig. 3f can be attributed to lattice oxygen and adsorbed oxygen [47]. It was observed that the lattice oxygen increased from 31.82% to 37.48% after oxidation. Adsorption and release of lattice oxygen is the rate-determining step in redox reaction [48]. Therefore, the increase of active lattice oxygen can improve the re-oxidation performance [25].

3.4. Structural stability and formation mechanism

The voids evolution was further analyzed to reveal the structure formation mechanism and clarify its relationship with the reaction performance. As shown in Fig. 4a, not only the first redox occurs the structural transition (Fig. 3c), but the voids can still appear in multiple cycles. Moreover, the particle size increases rapidly with increasing cycle. This is due to the surface energy difference of different grain sizes driving the fusion of large grains and the merge of small grains into the large grains (Ostwald ripening) [49]. The crystal growth of Cu_{1.5}Mn_{1.5}O₄ conformed to the Kossel-Stranski model [50]. Under the actual growth conditions, the (111) crystal facet was assembled layer-by-layer resulting in the appearance of growth steps at the end. However, the void structure of Cu_{1.5}Mn_{1.5}O₄ on the specific surface could be clearly observed after different cycles, which was speculated to be related to the directional transport of oxygen ions. It was worth noting that the particles agglomerated and grew after multiple cycles, the large-sized particles still maintained this structure. It indicates that the voids keep stability, so the material has excellent cyclic reactivity (Fig. 2b and c). However, due to the sintering caused by repeated cycles at high temperature, the particle growth reduced the chemical reaction area, resulting in a slight decrease in the performance of Cu_{1.5}Mn_{1.5}O₄.

The redox processes are accompanied by the exchange of ions and electrons. These processes lead to the generation and diffusion of defects, which determine the crystal phase and morphology of the material and its subsequent chemical behavior. EDS mapping is used to analyze the surface of voids (Fig. 4b and S1). It was found that the Mn in Cu_{1.5}Mn_{1.5}O₄ was uniformly distributed, but Cu was enriched on the outer surface of the voids, indicating that the obvious migration of Cu cations occurred during the oxidation.

The ions diffusion of Cu_{1.5}Mn_{1.5}O₄ during the oxidation was simulated by MD. The nanoparticle model is constructed in three-dimensional space as shown in Fig. S2. To simulate the process of O atom transfer from Cu_{1.5}Mn_{1.5}O₄ to CuMnO₂, we artificially removed O atom from the outermost layer of Cu_{1.5}Mn_{1.5}O₄. The diffusion coefficient D of different atoms of Cu_{1.5}Mn_{1.5}O₄ at 850 °C was obtained by analyzing the mean square displacement (MSD) with the least square method based on Einstein relation. The MSD was calculated as:

$$\text{MSD} \equiv \langle \Delta \vec{r}^2(t) \rangle \equiv \frac{1}{N} \sum_{i=1}^N (\vec{r}_i(t) - \vec{r}_i(0))^2$$

MSD is proportional to the observation time t which tends to be infinity. The diffusion coefficient D was acquired by:

$$D \equiv \frac{1}{6} \lim_{t \rightarrow \infty} \frac{\langle [r(t_0 + t) - r(t_0)]^2 \rangle}{t}$$

Here, $r_i(t)$ is the position of the atom at time t; N is the total number in the supercell; and the symbol $\langle \rangle$ indicate an ensemble average has been taken. The ensemble average is an average over all atoms.

By recording the position of the atom as a function of time, we calculated the MSD. The model after atom diffusion at oxidation temperature (850 °C) and the MSD curves over time are shown in Fig. 4c and d, respectively. The MSD-Time curves had great linear relations after

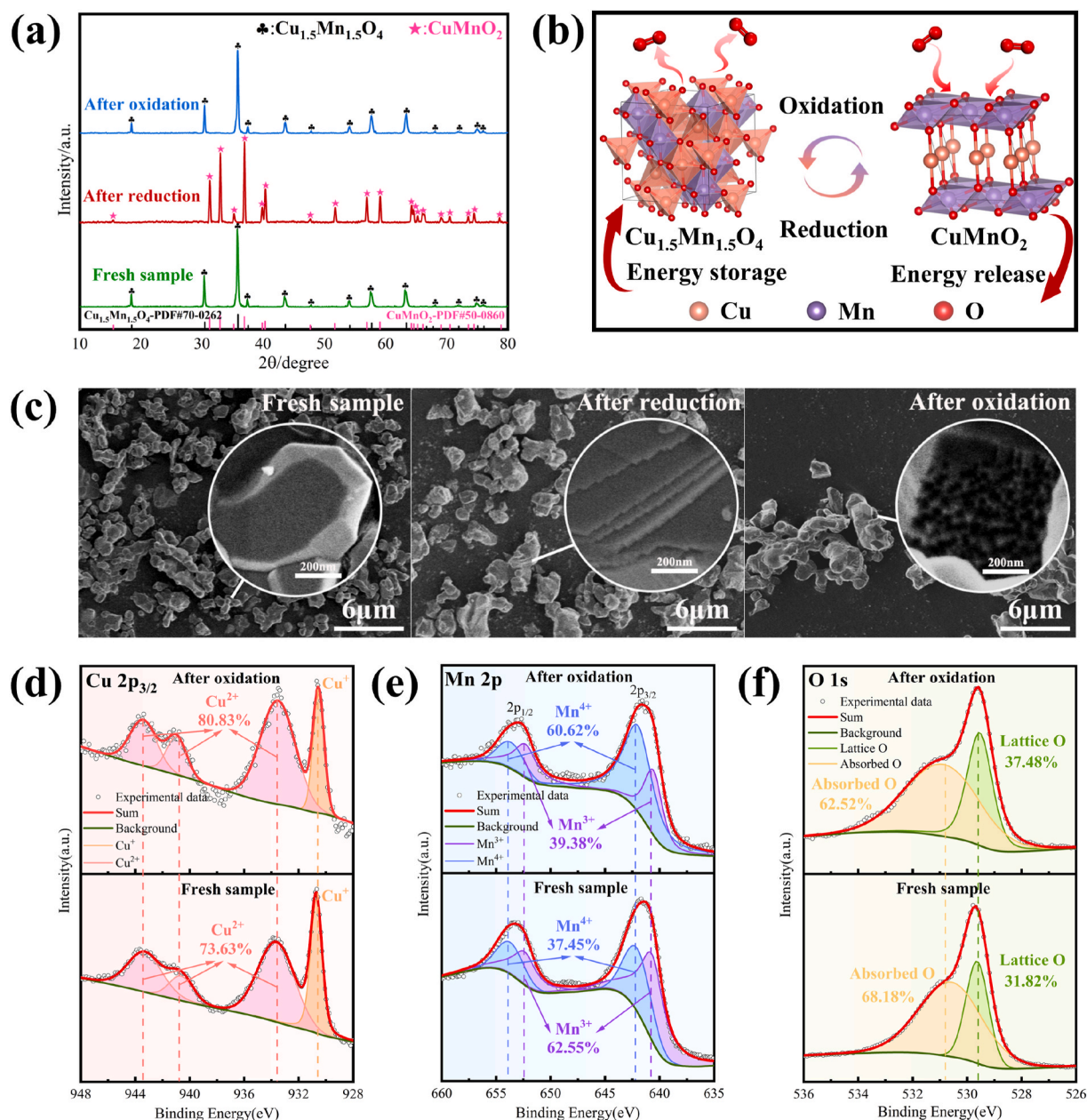


Fig. 3. Evolution of the structure and micromorphology during redox. (a) XRD patterns. (b) Schematic of phase transition. (c) FESEM images of the samples at different stages. XPS (d) Cu 2p_{3/2}, (e) Mn 2p, and (f) O 1s of fresh and oxidized samples.

100 ps, and D was calculated by fitting the slope. D_{Cu} ($7.4 \times 10^{-14} \text{ cm}^2 \text{ s}^{-1}$) was higher than D_{Mn} ($5.1 \times 10^{-14} \text{ cm}^2 \text{ s}^{-1}$) and D_{O} ($1.7 \times 10^{-14} \text{ cm}^2 \text{ s}^{-1}$), which was consistent with the experimental observation (Fig. 4b and S1).

This phenomenon can be attributed to the Kirkendall effect [51] (Fig. 4e). When the surface of CuMnO_2 was gradually oxidized to $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$, ions diffused along the crystal facet (111) perpendicular to the $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ product layer, providing O^{2-} for the internal unreacted CuMnO_2 until the oxidation was complete. However, the outward diffusion of Cu and Mn cations was faster than the inward diffusion of O anions through vacancy-assisted exchange. Accordingly, the resulting unequal diffusion was balanced by oppositely diffused vacancies, which could condense into voids at dislocations. Therefore, voids on the specific surface of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ appeared. In addition, the surface aggregation of Cu cations is speculated to be due to the fact that Cu ions on the surface are more likely to react with O (vs. Mn ions), resulting in the concentration gradient of Cu ions in $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$. And

the volume expansion of oxidation creates the physical space for ion diffusion, so that Cu ions transport outward faster. The particular structure can be described by the complex interaction of oxidation process, ion diffusion kinetics and mechanical expansion.

It is difficult to detect the effect of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ (111) surface termination on structure formation and ion diffusion by experimental characterization. However, one of the main mechanisms controlling structure formation and evolution is surface energy and diffusion in solid [52]. The minimum surface energy is the driving force for structure formation, and the diffusion determines the structure evolution. Therefore, the slab model optimization of different terminations on (111) surface of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ was further explored by DFT calculation. The results in Fig. 5a show that the Cu termination has the lowest surface energy of 1.194 J/m^2 , compared to the Mn termination (including a small amount of Cu). It indicated that it was the most stable surface structure of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$. The surface composed of Cu termination is easily exposed to the environment, so O anions are more easily bonded

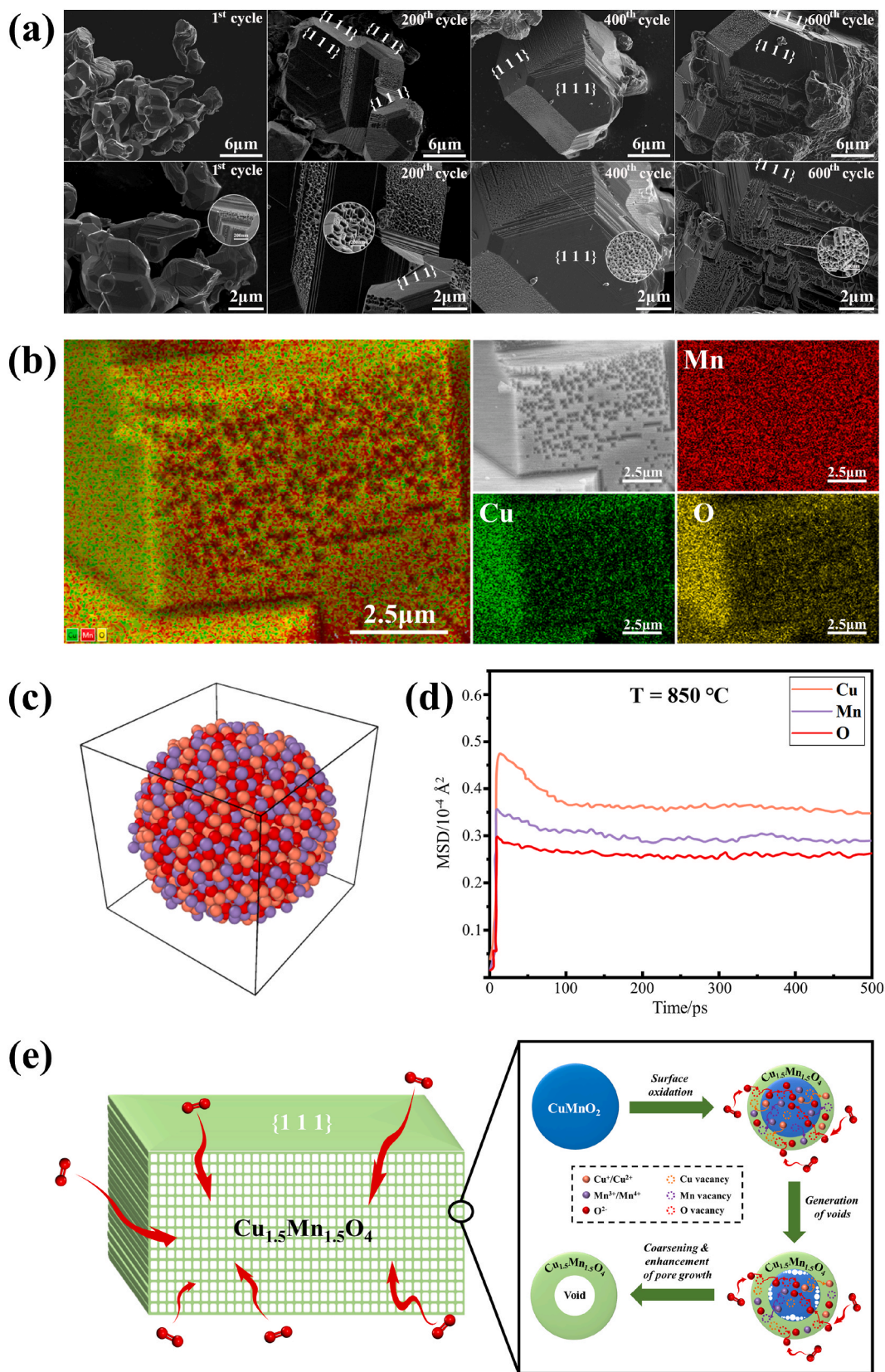


Fig. 4. The cyclic structural stability and formation mechanism of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$. (a) FESEM images of the samples at different cycles. (b) SEM images and corresponding EDS mapping of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ on directional void surface. (c) Model after atomic diffusion. (d) Mean square displacements (MSD) of different atoms in $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ versus time at 850 °C (Oxidation peak temperature). (e) Schematic of detailed formation mechanism of nanovoids by Kirkendall effect during the oxidation.

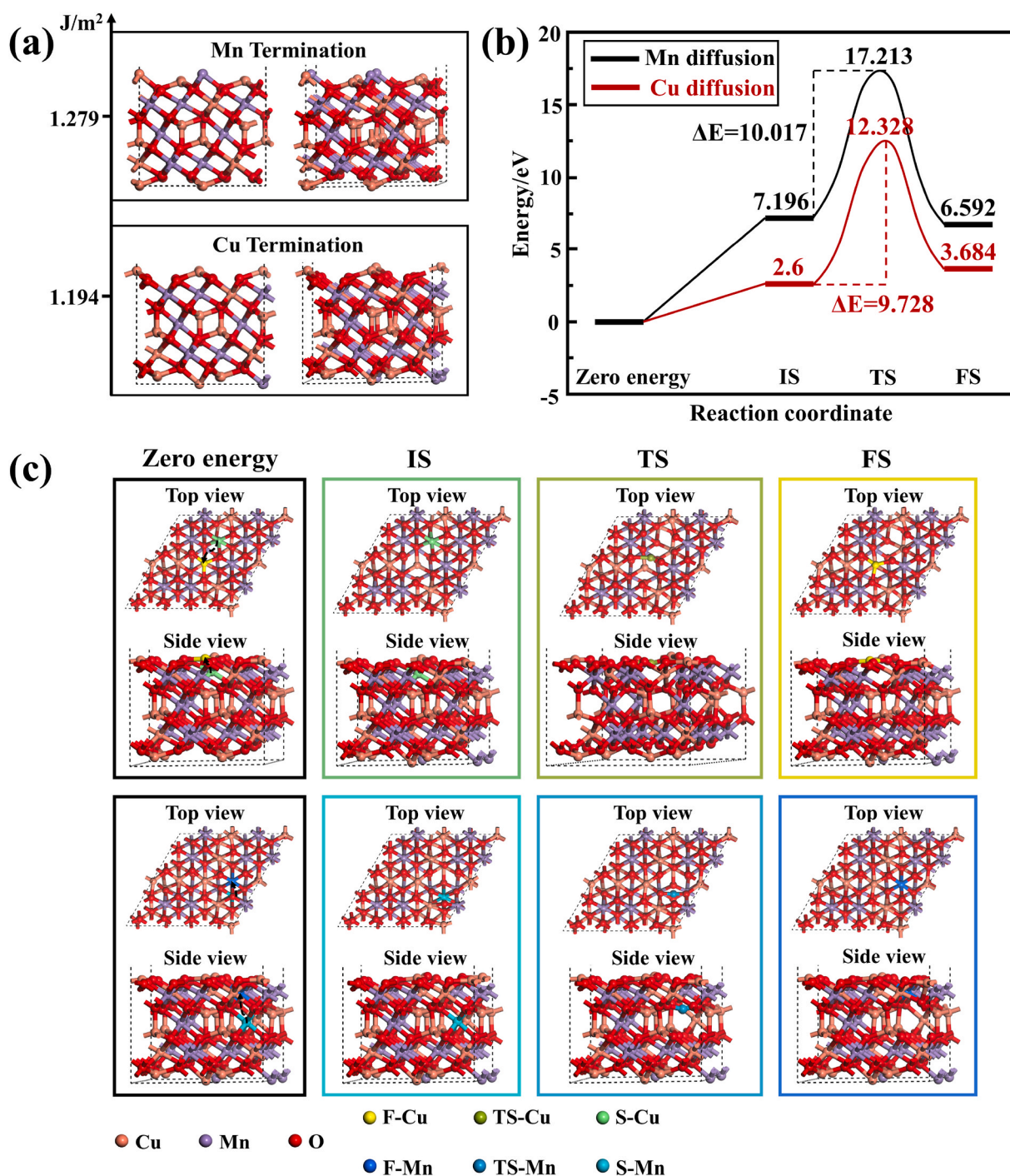


Fig. 5. Computation of surface structure growth and cation diffusion of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ by DFT. (a) Comparison of surface energy (E_{surf}) of different terminals on (111) surface. (b) Vacancy formation energies and diffusion energy barriers (ΔE) of Cu and Mn cations. (c) Cu and Mn diffusion pathways on (111) surface of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$. The zero energy corresponds to the complete slab model without vacancy. IS, TS and FS refer to the initial, transition and final states, respectively. The ions in the first atomic layer are labeled with “F” and in the second atomic layer with “S”.

with Cu cations, which is consistent with the results in Fig. 4b and S1. In addition, the vacancy formation energies of Cu and Mn at different sites of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ are shown in Figs. S3 and S4. Thus, the outward transport pathways of Cu and Mn cations are determined and the diffusion energy barrier (ΔE) is calculated, as shown in Fig. 5b and c. The vacancy formation energy ($E(V_{\text{Mn}}) = 7.196$ eV and 6.592 eV) in different layers and the diffusion energy barrier ($\Delta E = 10.017$ eV) of Mn were higher than those of Cu ($E(V_{\text{Cu}}) = 2.6$ eV and 3.684 eV, $\Delta E = 9.728$ eV). It shows that Cu cations are easier to diffuse than Mn cations, which results are in agreement with Fig. 4d, which helps to explain the

aggregation of Cu on the surface (Fig. 4b and S1).

3.5. Oxygen ion directional transport mechanism

Fig. 4a shows that $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ only generates the void structure on the specific surface, so the directional oxygen ion transport mechanism of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$ is further verified by DFT calculation. Low-index surfaces are easily exposed to the environment, so (100) and (110) are selected for comparison with (111). The surface energy (E_{surf}) of different terminals of (100) and (110) are shown in Figs. S5 and S6. The

optimized structure with the lowest surface energy was used for calculation.

The oxygen vacancy formation energies at different positions on different surfaces are appeared in Figs. S7–S9. O^{2-} diffuses into the interior through oxygen vacancies. Fig. 6a and S10 demonstrate the adsorption energies and models on (100), (110) and (111) surfaces. The adsorption energy on (100) surface was 0.225 eV, indicating that the adsorption process was endothermic and unstable. However, O^{2-} had the strongest adsorption capacity (−0.446 eV) and the most stable structure on (111) surface, elucidating that O^{2-} preferentially adsorbed on the (111) surface. The oxygen diffusion paths and calculation results on different surfaces are shown in Fig. 6b and c and S11–S13, respectively. Compared with (100) (2.349 eV) and (110) (2.083 eV), the oxygen vacancy formation energy $E(V_O)$ in the outermost layer of (111) was the lowest (0.512 eV). It indicated that the (111) surface promoted the formation of surface oxygen vacancies, providing active sites for surface reactions. In addition, the $E(V_O)$ in the bulk (1.765 eV) and oxygen migration energy barrier ΔE (4.5 eV) of (111) were lower than those of (100) ($E(V_O) = 2.309$ eV, $\Delta E = 6.667$ eV) and (110) ($E(V_O) = 1.811$ eV, $\Delta E = 4.989$ eV), elucidating that the oxygen vacancies inside the crystal also were also easier to generate and were conducive to improving oxygen ion diffusion kinetics. When the gas-solid reaction enters the diffusion stage through product layer, the diffusion of ions through the solid product becomes the main limiting factor of the reaction [53]. Therefore, the diffusion of O^{2-} in $Cu_{1.5}Mn_{1.5}O_4$ determined the redox reactivity. These results showed that the formation of oxygen vacancies through the inward diffusion of oxygen ions was easier on

(111) than other surfaces during the reaction to form the porous surface, which explained the experiments. Therefore, the (111) surface of $Cu_{1.5}Mn_{1.5}O_4$ was the optimal transport path of oxygen ions during redox. Combined with the difference in ion diffusion rate, the directional voids was created, which was conducive to improving the reactivity and accelerating the reaction kinetics.

4. Conclusion

In summary, we have successfully prepared $Cu_{1.5}Mn_{1.5}O_4$ with spinel structure containing Cu^+/Cu^{2+} and Mn^{3+}/Mn^{4+} mixed valence states. It had high energy storage and release density (−219.852 kJ/kg and 207.618 kJ/kg) and excellent chemical reversibility. And the reduction and oxidation conversion rates kept 97.06% and 92.98% of the initial capacity after 600 cycles, respectively. The experiment found that the spinel $Cu_{1.5}Mn_{1.5}O_4$ and layered $CuMnO_2$ undergo reversible phase transitions during redox. Surprisingly, $Cu_{1.5}Mn_{1.5}O_4$ appeared the special void structure after one cycle, but not in the fresh sample. The nanostructure effectively increased the chemical reaction area and provided abundant Cu^{2+} and Mn^{4+} species and lattice oxygen for $Cu_{1.5}Mn_{1.5}O_4$, which was beneficial to promote the redox reactivity. Further structural evolution analysis showed that Cu ions migrated significantly. And the D_{Cu} was higher than D_{Mn} and D_O by MD simulation. The structure formation mechanism was related to the Kirkendall effect. DFT calculations was used to further verify the aggregation of Cu element on the surface and void formation mechanism. In addition, $Cu_{1.5}Mn_{1.5}O_4$ was observed to have voids on specific surfaces. DFT

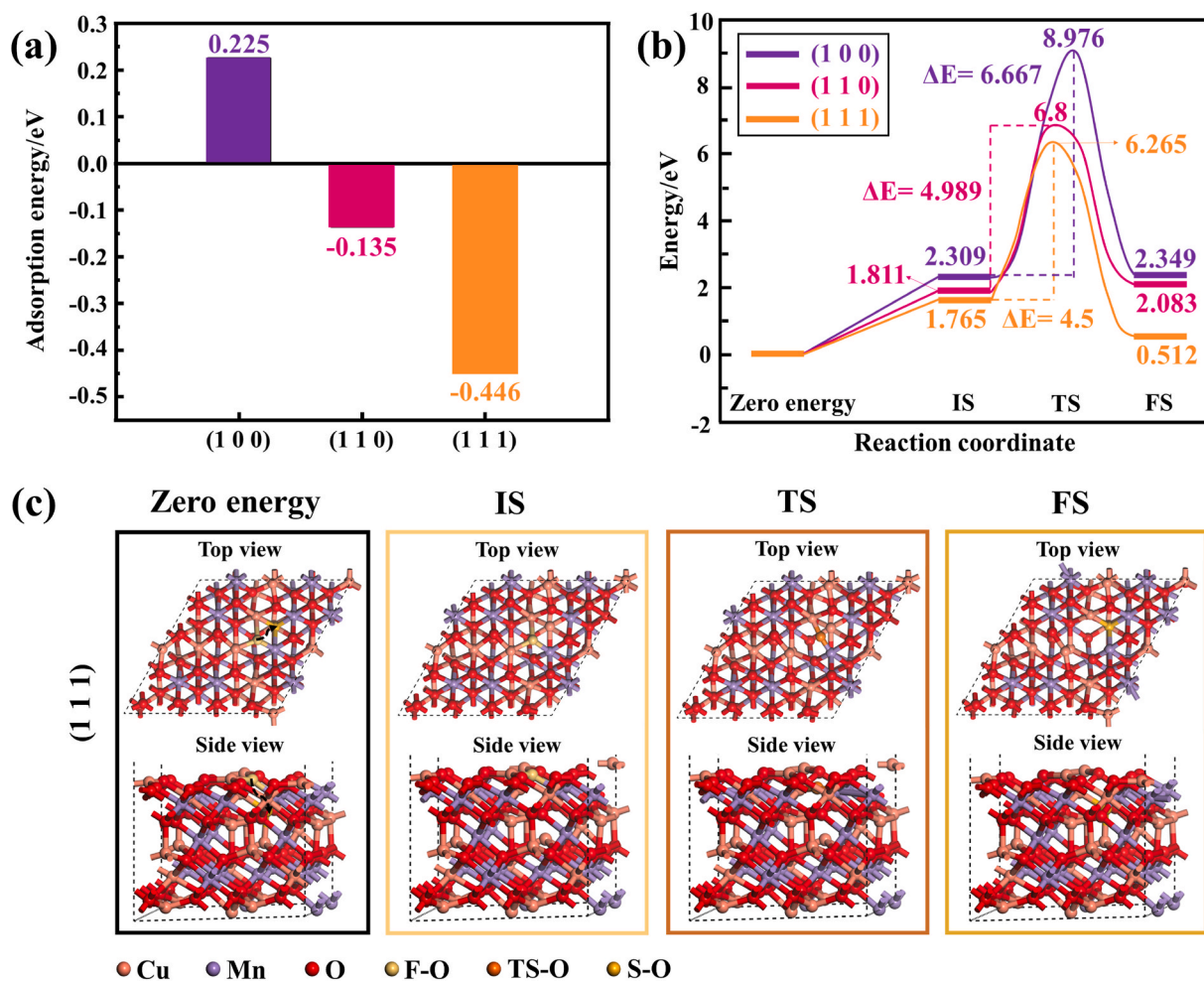


Fig. 6. DFT calculations results of directional oxygen ion diffusion. (a) Adsorption energies of O^{2-} on (100), (110) and (111) surfaces. (b) Oxygen vacancy formation energies $E(V_O)$ and diffusion energy barriers ΔE on different surfaces. (c) O diffusion pathway on (111) surface of $Cu_{1.5}Mn_{1.5}O_4$.

calculation proved that (111) surface was the optimal transport path of oxygen ions, resulting in directional voids that provide active sites for surface reactions and improve oxygen ion diffusion. Combined with experiments and calculations, we revealed the relationship between morphology changes and ion diffusion during the redox of $\text{Cu}_{1.5}\text{Mn}_{1.5}\text{O}_4$, clarified the optimal directional transport mechanism of oxygen ions, and analyzed their impact on performance improvement. This work provides an idea for the development and optimization of high-performance thermochemical energy storage materials. Through appropriate element doping, ion diffusion rate difference and optimal transport of oxygen ions can be generated, thereby creating directional voids to improve redox activity.

CRedit authorship contribution statement

Jiali Deng: Writing – original draft, Software, Methodology, Investigation, Conceptualization. **Changdong Gu:** Writing – review & editing, Validation. **Haoran Xu:** Writing – review & editing, Visualization. **Gang Xiao:** Supervision, Resources, Project administration, Funding acquisition.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Data availability

Data will be made available on request.

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Appendix A. Supplementary data

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